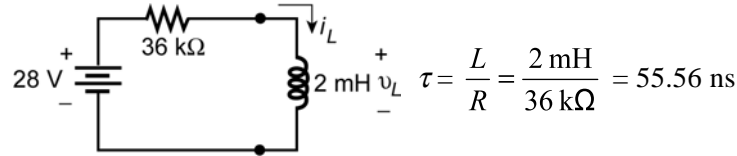


$$i_L = 1.3 \text{ mA}(1 - e^{-t/7.56\mu\text{s}})$$

$$v_L = 8.09 \text{ V}e^{-t/7.56\mu\text{s}}$$

b. $0.632(1.3 \text{ mA}) = \mathbf{0.822 \text{ mA}}$
 $0.368(8.09 \text{ V}) = \mathbf{2.98 \text{ V}}$

24. a. Source conversion: $E = IR = (4 \text{ mA})(12 \text{ k}\Omega) = 48 \text{ V}$, $E_{\text{Net}} = 48 \text{ V} - 20 \text{ V} = 28 \text{ V}$



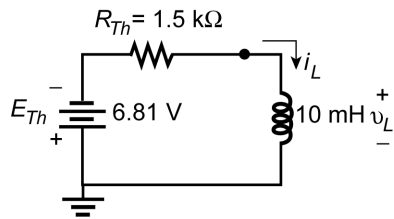
$$i_L = \frac{E}{R}(1 - e^{-t/\tau}) = \frac{28 \text{ V}}{36 \text{ k}\Omega}(1 - e^{-t/\tau}) = \mathbf{0.778 \text{ mA}(1 - e^{-t/55.56\text{ns}})}$$

$$v_L = Ee^{-t/\tau} = \mathbf{28 \text{ V}e^{-t/55.56\text{ns}}}$$

b. $t = 100 \text{ ns}$:
 $i_L = 0.778 \text{ mA}(1 - e^{-100\text{ns}/55.56\text{ns}}) = 0.778 \text{ mA}(1 - \underbrace{e^{-1.8}}_{0.165}) = \mathbf{0.65 \text{ mA}}$

$$v_L = 28 \text{ V}e^{-1.8} = \mathbf{4.62 \text{ V}}$$

25. a.



$$R_{Th} = 2.2 \text{ k}\Omega \parallel 4.7 \text{ k}\Omega = 1.50 \text{ k}\Omega$$

$$E_{Th} = -\frac{4.7 \text{ k}\Omega(10 \text{ V})}{4.7 \text{ k}\Omega + 2.2 \text{ k}\Omega} = -6.81 \text{ V}$$

$$\tau = \frac{L}{R} = \frac{10 \text{ mH}}{1.50 \text{ k}\Omega} = 6.67 \mu\text{s}$$

$$i_L = -\frac{E}{R}(1 - e^{-t/\tau}) = -\frac{6.81 \text{ V}}{1.5 \text{ k}\Omega}(1 - e^{-t/\tau}) = \mathbf{-4.54 \text{ mA}(1 - e^{-t/6.67\mu\text{s}})}$$

$$v_L = Ee^{-t/\tau} = -E_{Th}e^{-t/\tau} = \mathbf{-6.81 \text{ V}e^{-t/6.67\mu\text{s}}}$$

b. $t = 10 \mu\text{s}$:
 $i_L = -4.54 \text{ mA}(1 - e^{-10\mu\text{s}/6.67\mu\text{s}}) = -4.54 \text{ mA}(1 - \underbrace{e^{-1.5}}_{0.223})$

$$= \mathbf{-3.53 \text{ mA}}$$

$$v_L = -6.81 \text{ V}(0.223) = \mathbf{-1.52 \text{ V}}$$

c. $\tau = \frac{L}{R} = \frac{10 \text{ mH}}{4.7 \text{ k}\Omega} = 2.13 \mu\text{s}$

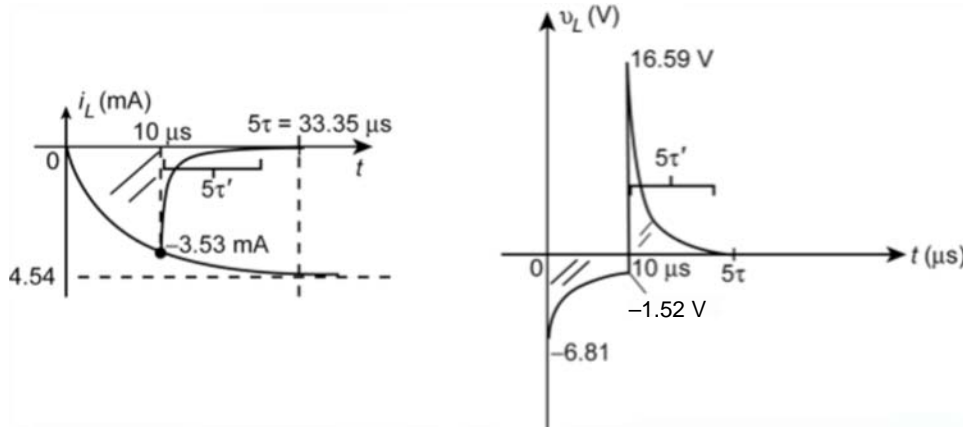
$$i_L = \mathbf{-3.53 \text{ mA}e^{-t/2.13\mu\text{s}}}$$

At $t = 10 \mu\text{s}$

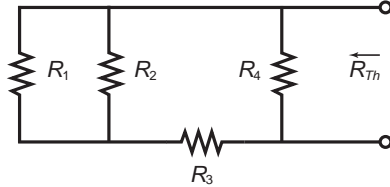
$$V_L = (3.53 \text{ mA})(4.7 \text{ k}\Omega) = 16.59 \text{ V}$$

$$v_L = \mathbf{16.59 \text{ V}e^{-t/2.13\mu\text{s}}}$$

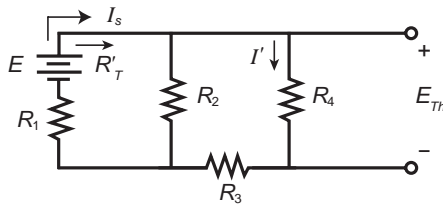
d.



26. a. Finding the Thevenin circuit for the inductor:



$$\begin{aligned} R_{Th} &= R_4 \parallel (R_3 + R_1 \parallel R_2) \\ &= 1 \text{ k}\Omega \parallel (2.7 \text{ k}\Omega + 8.2 \text{ k}\Omega \parallel 2.2 \text{ k}\Omega) \\ &= 1 \text{ k}\Omega \parallel 4.43 \text{ k}\Omega \\ &= 0.816 \text{ k}\Omega \end{aligned}$$

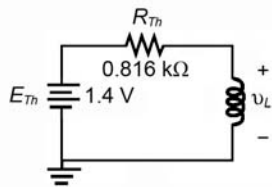


$$\begin{aligned} R_T' &= R_1 + R_2 \parallel (R_3 + R_4) \\ &= 8.2 \text{ k}\Omega + 2.2 \text{ k}\Omega \parallel (2.7 \text{ k}\Omega + 1 \text{ k}\Omega) \\ &= 8.2 \text{ k}\Omega + 2.2 \text{ k}\Omega \parallel 3.7 \text{ k}\Omega \\ &= 8.2 \text{ k}\Omega + 1.38 \text{ k}\Omega \\ &= 9.58 \text{ k}\Omega \end{aligned}$$

$$\text{Then } I_s = \frac{E}{R_T'} = \frac{36 \text{ V}}{9.58 \text{ k}\Omega} = 3.76 \text{ mA}$$

$$\text{and } I' = \frac{R_2(I_s)}{R_2 + R_3 + R_4} = \frac{2.2 \text{ k}\Omega(3.76 \text{ mA})}{2.2 \text{ k}\Omega + 2.7 \text{ k}\Omega + 1 \text{ k}\Omega} = 1.4 \text{ mA}$$

$$\text{and finally } E_{Th} = I'R_4 = (1.4 \text{ mA})(1 \text{ k}\Omega) = 1.4 \text{ V}$$

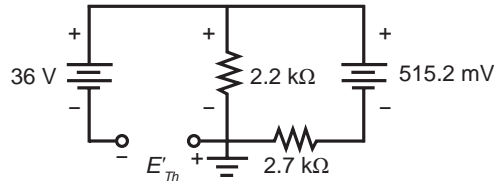
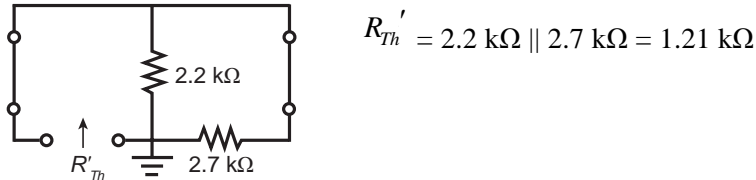
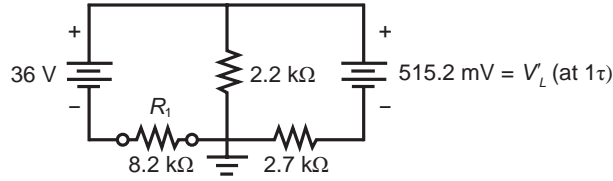


$$\begin{aligned} \tau &= \frac{L}{R} = \frac{10 \text{ mH}}{0.816 \text{ k}\Omega} = 12.25 \mu\text{s} \\ v_L &= 1.4 \text{ V} e^{-t/12.25\mu\text{s}} \\ &= 1.4 \text{ V} e^{-25\mu\text{s}/12.25\mu\text{s}} \\ &= 1.4 \text{ V} e^{-2.05} \\ &= 1.4 \text{ V}(128.73 \times 10^{-3}) \\ &= \mathbf{180 \text{ mV}} \end{aligned}$$

b.

$$\begin{aligned} v_L &= 1.4 \text{ V} e^{-t/12.25\mu\text{s}} \\ v_L &= 1.4 \text{ V} e^{-1\mu\text{s}/12.25\mu\text{s}} \\ &= (1.4 \text{ V})(e^{-0.082}) \\ &= (1.4 \text{ V})(.921) \\ &= \mathbf{1.29 \text{ V}} \end{aligned}$$

- c. Finding the Thevenin equivalent for R_1 at 1τ
 At 1τ : $v_L = 1.4 \text{ V} e^{-t/\tau} = 1.4 \text{ V} e^{-1} = 1.4 \text{ V} (0.368) = 515.2 \text{ mV}$

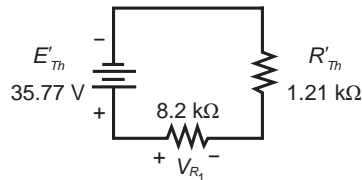


$$-E'_{Th} + 36 \text{ V} - v_{R_2} = 0$$

$$E'_{Th} = 36 - v_{R_2}$$

$$v_{R_2} = \frac{2.2 \text{ k}\Omega(515.2 \text{ mV})}{2.2 \text{ k}\Omega + 2.7 \text{ k}\Omega} = 0.231 \text{ V}$$

$$\therefore E'_{Th} = 36 \text{ V} - 0.231 \text{ V} = 35.77 \text{ V}$$



$$v_{R_1} = \frac{8.2 \text{ k}\Omega(35.77 \text{ V})}{8.2 \text{ k}\Omega + 1.21 \text{ k}\Omega} = \mathbf{31.34 \text{ V}}$$

d.
$$i_L = \frac{E_{Th}}{R_{Th}} (1 - e^{-t/\tau})$$

$$= \frac{1.4 \text{ V}}{0.81 \text{ k}\Omega} (1 - e^{-t/12.25 \mu\text{s}})$$

$$= 1.72 \text{ mA} (1 - e^{-t/12.25 \mu\text{s}})$$

$$1 \text{ mA} = 1.72 \text{ mA} (1 - e^{-t/12.25 \mu\text{s}})$$

$$0.581 = 1 - e^{-t/12.25 \mu\text{s}}$$

$$0.419 = e^{-t/12.25 \mu\text{s}}$$

$$t = 12.25 \mu\text{s} \log_e 0.419$$

$$= 12.25 \mu\text{s} (0.87)$$

$$= \mathbf{10.66 \mu\text{s}}$$

27. a.
$$I_i = \frac{16 \text{ V}}{4.7 \text{ k}\Omega + 3.3 \text{ k}\Omega} = 2 \text{ mA}$$

$t = 0 \text{ s}$: Thevenin:

$$R_{Th} = 3.3 \text{ k}\Omega + 1 \text{ k}\Omega \parallel 4.7 \text{ k}\Omega = 3.3 \text{ k}\Omega + 0.82 \text{ k}\Omega = 4.12 \text{ k}\Omega$$

$$E_{Th} = \frac{1 \text{ k}\Omega(16 \text{ V})}{1 \text{ k}\Omega + 4.7 \text{ k}\Omega} = 2.81 \text{ V}$$

$$i_L = I_f + (I_i - I_f)e^{-t/\tau}$$

$$I_f = \frac{2.81 \text{ V}}{4.12 \text{ k}\Omega} = 0.68 \text{ mA}, \quad \tau = \frac{L}{R} = \frac{2 \text{ H}}{4.12 \text{ k}\Omega} = 0.49 \text{ ms}$$

$$i_L = 0.68 \text{ mA} + (2 \text{ mA} - 0.68 \text{ mA})e^{-t/0.49 \text{ ms}}$$

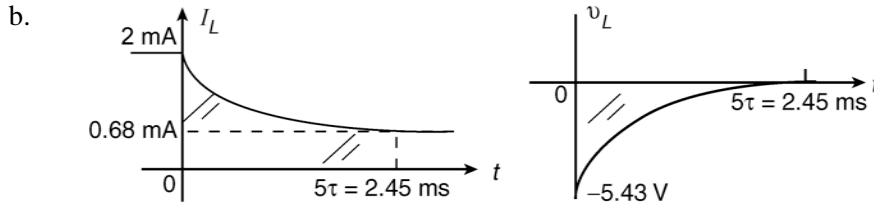
$$i_L = \mathbf{0.68 \text{ mA} + 1.32 \text{ mA}e^{-t/0.49 \text{ ms}}}$$

$$v_R(0+) = 2 \text{ mA}(4.12 \text{ k}\Omega) = 8.24 \text{ V}$$

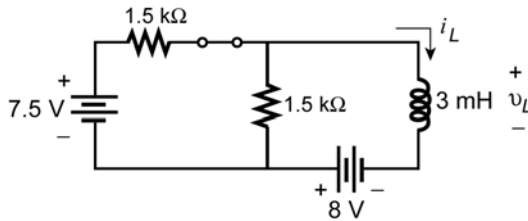
$$\text{KVL}(0+): \quad 2.81 \text{ V} - 8.24 \text{ V} - v_L = 0$$

$$v_L = -5.43 \text{ V}$$

$$v_L = \mathbf{-5.43 \text{ V}e^{-t/0.49 \text{ ms}}}$$

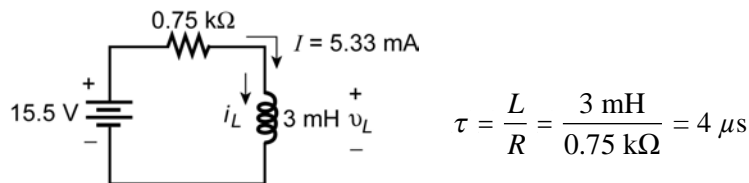


28. a. Steady-state: $I_L = \frac{8 \text{ V}}{1.5 \text{ k}\Omega} = 5.33 \text{ mA}$, $V_L = 0 \text{ V}$
 $R_{Th} = (3 \text{ k}\Omega \parallel 12 \text{ k}\Omega) \parallel 4 \text{ k}\Omega = 1.5 \text{ k}\Omega$
 $E_{Th} = \frac{2.4 \text{ k}\Omega(20 \text{ V})}{2.4 \text{ k}\Omega + 4 \text{ k}\Omega} = 7.5 \text{ V}$



$$R'_{Th} = 1.5 \text{ k}\Omega \parallel 1.5 \text{ k}\Omega = 0.75 \text{ k}\Omega$$

$$E'_{Th} = 8 \text{ V} + 7.5 \text{ V} = 15.5 \text{ V}$$



$$I_f = \frac{15.5 \text{ V}}{0.75 \text{ k}\Omega} = 20.67 \text{ mA} \quad I_i = 5.33 \text{ mA}$$

$$i_L = I_f + (I_i - I_f)e^{-t/\tau}$$

$$= 20.67 \text{ mA} + (5.33 \text{ mA} - 20.67 \text{ mA})e^{-t/4 \mu\text{s}}$$

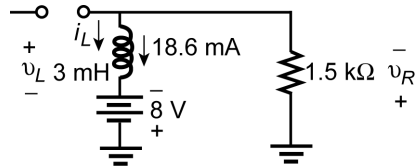
$$i_L = \mathbf{20.67 \text{ mA} - 15.34 \text{ mA}e^{-t/4 \mu\text{s}}}$$

$$v_L = \mathbf{15.5 \text{ V}e^{-t/4 \mu\text{s}}}$$

b. $i_L(2\tau) = 20.67 \text{ mA} - 15.34 \text{ mA} \underbrace{e^{-2}}_{0.135}$
 $= \mathbf{18.6 \text{ mA}}$

$v_L(2\tau) = 15.5 \text{ V} e^{-2} = 15.5 \text{ V}(0.135) = \mathbf{2.09 \text{ V}}$

c. $I_i = 18.6 \text{ mA}$



$$v_L + v_R - 8 \text{ V} = 0$$

$$v_L = 8 \text{ V} - v_R = 8 \text{ V} - (18.6 \text{ mA})(1.5 \text{ k}\Omega)$$

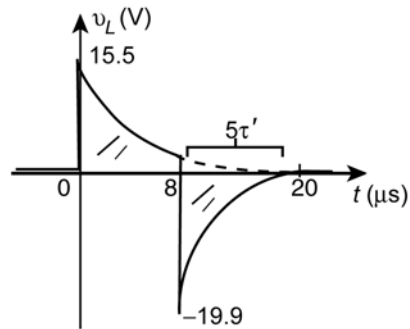
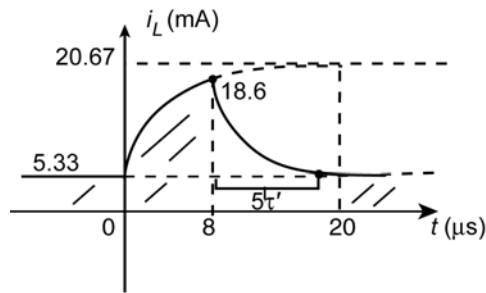
$$= -19.9 \text{ V}$$

$$\tau' = \frac{L}{R} = \frac{3 \text{ mH}}{1.5 \text{ k}\Omega} = 2 \mu\text{s}$$

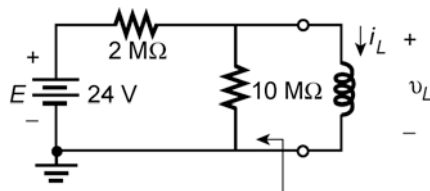
$I_i = 18.6 \text{ mA}$ $I_f = \frac{8 \text{ V}}{1.5 \text{ k}\Omega} = 5.33 \text{ mA}$

$i_L = I_f + (I_i - I_f)e^{-t/\tau} = 5.33 \text{ mA} + (18.6 \text{ mA} - 5.33 \text{ mA})e^{-t/2\mu\text{s}}$
 $= \mathbf{5.33 \text{ mA} + 13.27 \text{ mA}e^{-t/2\mu\text{s}}}$

$v_L = -\mathbf{19.9 \text{ V}e^{-t/2\mu\text{s}}}$



29. a.



$R_{Th} = 2 \text{ M}\Omega \parallel 10 \text{ M}\Omega = 1.67 \text{ M}\Omega$

$E_{Th} = \frac{10 \text{ M}\Omega(24 \text{ V})}{10 \text{ M}\Omega + 2 \text{ M}\Omega} = 20 \text{ V}$

$I_L(0^-) = \frac{E_{Th}}{R_{Th}} = \frac{20 \text{ V}}{1.67 \text{ M}\Omega} = \mathbf{12 \mu\text{A}}$

$\tau' = \frac{L}{R_{\text{meter}}} = \frac{5 \text{ H}}{10 \text{ M}\Omega} = 5 \mu\text{s}$

$i_L = 12 \mu\text{A}e^{-t/5 \mu\text{s}}$
 $10 \mu\text{A} = 12 \mu\text{A}e^{-t/5 \mu\text{s}}$

$$0.833 = e^{-t/5 \mu s}$$

$$\log_e 0.833 = -t/5 \mu s$$

$$0.183 = t/5 \mu s$$

$$t = 0.183(5 \mu s) = \mathbf{0.92 \mu s}$$

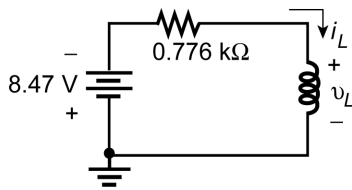
b. $v_L(0^+) = i_L(0^+)R_m = (12 \mu A)(10 M\Omega) = 120 V$
 $v_L = 120 V e^{-t/5 \mu s} = 120 V e^{-10 \mu s/5 \mu s} = 120 V e^{-2} = 120 V(0.135) = \mathbf{16.2 V}$

c. $v_L = 120 V e^{-5t/\tau} = 120 V e^{-5} = 120 V(6.74 \times 10^{-3}) = \mathbf{0.81 V}$

30. a. Closed Switch:

$$R_{Th} = 1.2 \text{ k}\Omega \parallel 2.2 \text{ k}\Omega = 0.776 \text{ k}\Omega$$

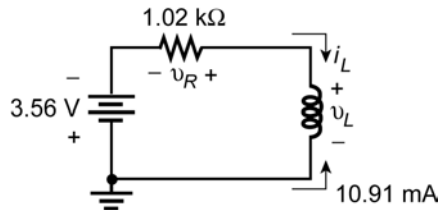
$$E_{Th} = \frac{1.2 \text{ k}\Omega(24 \text{ V})}{1.2 \text{ k}\Omega + 2.2 \text{ k}\Omega} = 8.47 \text{ V}$$



Open Switch:

$$R'_{Th} = 6.9 \text{ k}\Omega \parallel 1.2 \text{ k}\Omega = 1.02 \text{ k}\Omega$$

$$E'_{Th} = \frac{1.2 \text{ k}\Omega(24 \text{ V})}{8.1 \text{ k}\Omega} = -3.56 \text{ V}$$



$$-3.56 \text{ V} + v_R - v_L = 0$$

$$v_L = -3.56 \text{ V} + (10.91 \text{ mA})(1.02 \text{ k}\Omega)$$

$$= 7.57 \text{ V}$$

$$v_L = 7.57 \text{ V} e^{-t/1.18 \text{ ms}}$$

$$\tau = \frac{L}{R} = \frac{1.24 \text{ H}}{1.02 \text{ k}\Omega} = 1.18 \text{ ms}$$

$$I_{ss} = \frac{3.56 \text{ V}}{1.02 \text{ k}\Omega} = 3.49 \text{ mA} = I_f$$

$$i_L = I_f + (I_i - I_f)e^{-t/\tau}$$

$$= -3.49 \text{ mA} + ((-10.91 \text{ mA} - (-3.49 \text{ mA}))e^{-t/1.18 \text{ ms}})$$

$$i_L = \mathbf{-3.49 \text{ mA} - 7.42 \text{ mA} e^{-t/1.18 \text{ ms}}}$$