

31. a.  $i_L = 100 \text{ mA}(1 - e^{-1\text{ms}/20\text{ms}}) = 100 \text{ mA}(1 - e^{-1/20})$   
 $= 100 \text{ mA}(1 - e^{-0.05}) = 100 \text{ mA}(1 - 951.23 \times 10^{-3}) = 100 \text{ mA}(48.77 \times 10^{-3})$   
 $= \mathbf{4.88 \text{ mA}}$
- b.  $i_L = 100 \text{ mA}(1 - e^{-100\text{ms}/20\text{ms}}) = 100 \text{ mA}(1 - e^{-5})$   
 $= \mathbf{99.33 \text{ mA}}$
- c.  $50 \text{ mA} = 100 \text{ mA}(1 - e^{-t/\tau})$   
 $0.5 = 1 - e^{-t/\tau}$   
 $-0.5 = -e^{-t/\tau}$   
 $0.5 = e^{-t/\tau}$   
 $\log_e 0.5 = -t/\tau$   
 $t = -(\tau)(\log_e 0.5) = -(20 \text{ ms})(\log_e 0.5) = -(20 \text{ ms})(-693.15 \times 10^{-3})$   
 $= \mathbf{13.86 \text{ ms}}$
- d.  $99 \text{ mA} = 100 \text{ mA}(1 - e^{-t/20 \text{ ms}})$   
 $0.99 = 1 - e^{-t/20\text{ms}}$   
 $-0.01 = -e^{-t/20\text{ms}}$   
 $0.01 = e^{-t/20\text{ms}}$   
 $\log_e 0.01 = -t/20 \text{ ms}$   
 $t = -(20 \text{ ms})(\log_e 0.01) = -(20 \text{ ms})(-4.605) = \mathbf{92.1\text{ms}}$

32. a.  $I_L(1\tau) = 0.632I_{\max} = 126.4 \mu\text{A}$   

$$I_{\max} = \frac{126.4}{0.632} = \mathbf{200 \mu\text{A}}$$

$$i_L = I_m(1 - e^{-t/\tau})$$

$$160 \mu\text{A} = 200 \mu\text{A} \left( 1 - e^{\frac{-64.4 \mu\text{s}}{\tau}} \right)$$

b. 
$$0.8 = 1 - e^{\frac{-64.4 \mu\text{s}}{\tau}}$$

$$0.2 = e^{\frac{-64.4 \mu\text{s}}{\tau}}$$

$$\log_e 0.2 = -1.61 = \frac{-64.4 \mu\text{s}}{\tau}$$

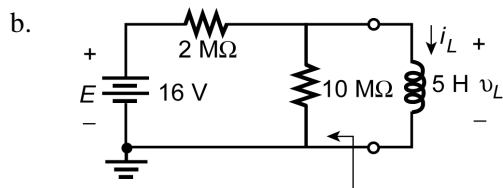
$$\tau = \frac{64.4 \mu\text{s}}{1.61} = \mathbf{40 \mu\text{s}}$$

c.  $\tau = \frac{L}{R} = 40 \mu\text{s} = \frac{L}{500 \text{ k}\Omega}$ ,  $L = (500 \text{ k}\Omega)(40 \mu\text{s}) = \mathbf{20 \text{ mH}}$

d.  $I_m = \frac{E}{R} \Rightarrow E = (200 \mu\text{A})(500 \Omega) = \mathbf{100 \text{ mV}}$

33. a.  $L \Rightarrow$  open circuit equivalent  

$$V_L = \frac{10 \text{ M}\Omega(16 \text{ V})}{10 \text{ M}\Omega + 2 \text{ M}\Omega} = \mathbf{13.33 \text{ V}}$$



$$R_{Th} = 2 \text{ M}\Omega \parallel 10 \text{ M}\Omega = 1.67 \text{ M}\Omega$$

$$E_{Th} = \frac{10 \text{ M}\Omega(16 \text{ V})}{10 \text{ M}\Omega + 2 \text{ M}\Omega} = 13.33 \text{ V}$$

$$I_{L_{\text{final}}} = \frac{E_{Th}}{R_{Th}} = \frac{13.33 \text{ V}}{1.67 \text{ M}\Omega} = \mathbf{7.98 \mu\text{A}}$$

c. 
$$i_L = 7.98 \mu\text{A}(1 - e^{-t/3 \mu\text{s}})$$
  $\tau = \frac{L}{R} = \frac{5 \text{ H}}{1.67 \text{ M}\Omega} = 3 \mu\text{s}$

$$10 \mu\text{A} = 7.98 \mu\text{A}(1 - e^{-t/3 \mu\text{s}})$$

$$1.253 = 1 - e^{-t/3 \mu\text{s}}$$

$$0.253 = e^{-t/3 \mu\text{s}}$$

$$\log_e(0.253) = -t/3 \mu\text{s}$$

$$1.374 = t/3 \mu\text{s}$$

$$t = 1.374(3 \mu\text{s}) = \mathbf{4.12 \mu\text{s}}$$

$$d. \quad v_L = 13.33 \text{ V } e^{-t/3 \mu\text{s}} = 13.33 \text{ V } e^{-12 \mu\text{s}/3 \mu\text{s}} = 13.33 \text{ V } e^{-4} \\ = 13.33 \text{ V}(0.0183) = \mathbf{0.244 \text{ V}}$$

$$34. \quad e_L = L \frac{\Delta i}{\Delta t} : \quad 0 - 4 \text{ ms}, e_L = (200 \text{ mH}) \left[ \frac{15 \text{ mA}}{4 \text{ ms}} \right] = \mathbf{750 \text{ mV}}$$

$$4 - 10 \text{ ms}, e_L = (200 \text{ mH}) \left[ \frac{0 \text{ mA}}{6 \text{ ms}} \right] = \mathbf{0 \text{ V}}$$

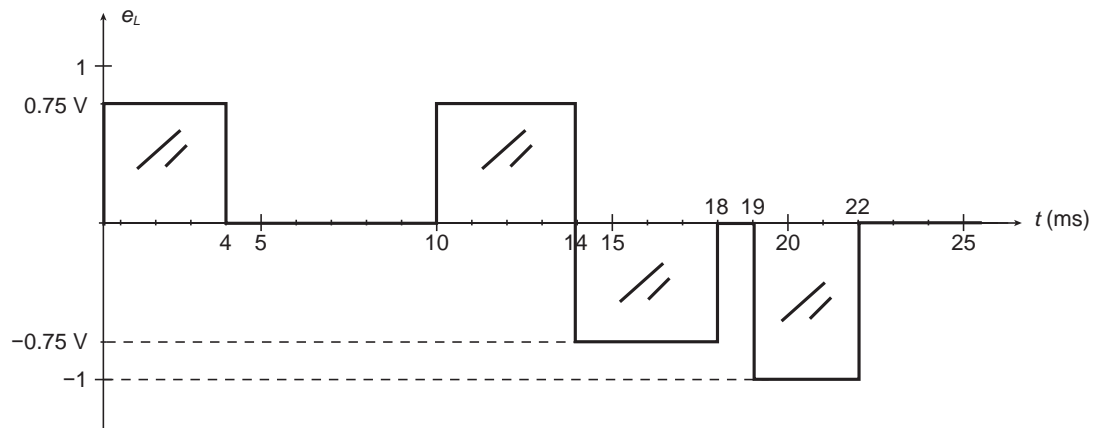
$$10 - 14 \text{ ms}, e_L = (200 \text{ mH}) \left[ \frac{15 \text{ mA}}{4 \text{ ms}} \right] = \mathbf{750 \text{ mV}}$$

$$14 - 18 \text{ ms}, e_L = -(200 \text{ mH}) \left[ \frac{15 \text{ mA}}{4 \text{ ms}} \right] = \mathbf{-750 \text{ mV}}$$

$$18 - 19 \text{ ms}, e_L = \mathbf{0 \text{ V}}$$

$$19 - 22 \text{ ms}, e_L = -(200 \text{ mH}) \left[ \frac{15 \text{ mA}}{3 \text{ ms}} \right] = \mathbf{-1 \text{ V}}$$

$$22 \text{ ms} \rightarrow, e_L = \mathbf{0 \text{ V}}$$



$$35. \quad v_L = L \frac{\Delta i_L}{\Delta t}$$

$$0 \rightarrow 2 \text{ ms}: v_L = \mathbf{0 \text{ V}}$$

$$2 \rightarrow 6 \text{ ms}: v_L = -(5 \text{ mH}) \left( \frac{30 \text{ mA}}{4 \text{ ms}} \right) = \mathbf{-37.5 \text{ mV}}$$

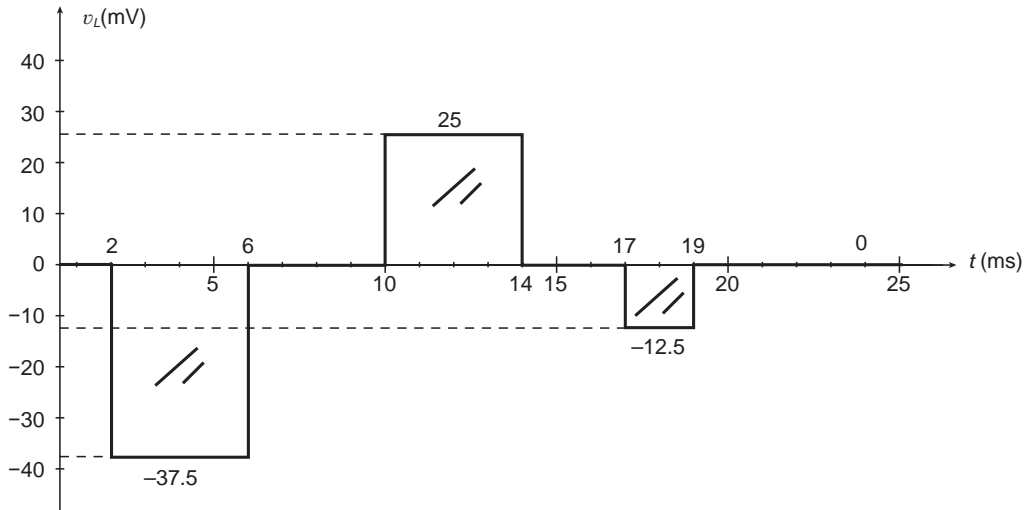
$$6 \rightarrow 10 \text{ ms}: v_L = \mathbf{0 \text{ V}}$$

$$10 \rightarrow 14 \text{ ms}: v_L = (5 \text{ mH}) \left( \frac{20 \text{ mA}}{4 \text{ ms}} \right) = \mathbf{25 \text{ mV}}$$

$$14 \rightarrow 17 \text{ ms}: v_L = \mathbf{0 \text{ V}}$$

$$17 \rightarrow 19 \text{ ms}: v_L = -(5 \text{ mH}) \left( \frac{5 \text{ mA}}{2 \text{ ms}} \right) = \mathbf{-12.5 \text{ mV}}$$

$$19 \rightarrow, v_L = \mathbf{0 \text{ V}}$$



36.  $L = 10 \text{ mH}$ ,  $4 \text{ mA}$  at  $t = 0 \text{ s}$

$$v_L = L \frac{\Delta i}{\Delta t} \Rightarrow \Delta i = \frac{\Delta t}{L} v_L$$

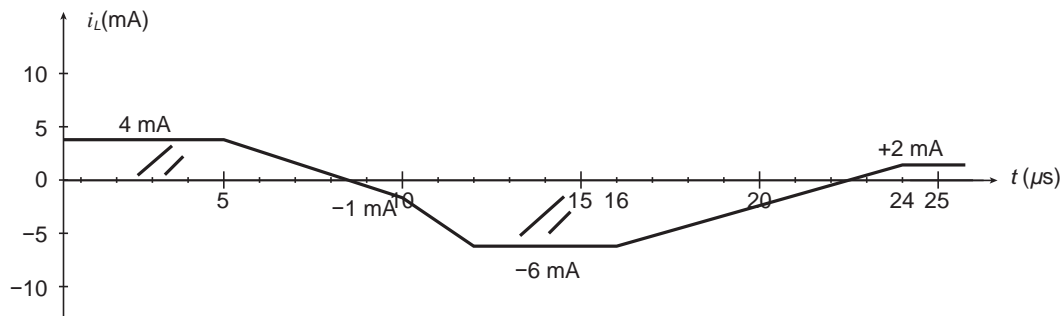
$0 - 5 \mu\text{s}$ :  $v_L = 0 \text{ V}$ ,  $\Delta i_L = 0 \text{ mA}$  and  $i_L = \mathbf{4 \text{ mA}}$

$$5 - 10 \mu\text{s}: \Delta i_L = \frac{5 \mu\text{s}}{10 \text{ mH}} (-10 \text{ V}) = \mathbf{-5 \text{ mA}}$$

$$10 - 12 \mu\text{s}: \Delta i_L = \frac{2 \mu\text{s}}{10 \text{ mH}} (-25 \text{ V}) = \mathbf{-5 \text{ mA}}$$

$12 - 16 \mu\text{s}$ :  $v_L = 0 \text{ V}$ ,  $\Delta i_L = 0 \text{ mA}$  and  $i_L = \mathbf{-6 \text{ mA}}$

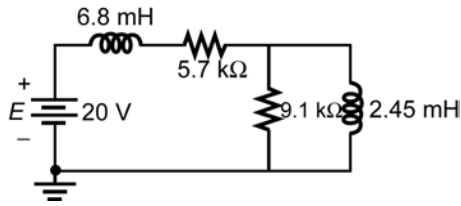
$$16 - 24 \mu\text{s}: \Delta i_L = \frac{8 \mu\text{s}}{10 \text{ mH}} 10 \text{ V} = \mathbf{8 \text{ mA}}$$



37. a.  $L_4 + L_5 = 5.6 \text{ mH} + 2 \text{ mH} = 7.6 \text{ mH}$   
 $L_3 \parallel 7.6 \text{ mH} = 3 \text{ mH} \parallel 7.6 \text{ mH} = 2.15 \text{ mH}$   
 $L_2 + 2.18 \text{ mH} = 3.3 \text{ mH} + 2.15 \text{ mH} = 5.45 \text{ mH}$   
 $L_1 \parallel 5.45 \text{ mH} = 2.4 \text{ mH} \parallel 5.45 \text{ mH} = 1.67 \text{ mH}$   
 $L_T = L_6 + 1.67 \text{ mH} = 9.1 \text{ mH} + 1.67 \text{ mH} = \mathbf{10.77 \text{ mH}}$

38.  $L_2 \parallel L_4 = 10 \text{ mH} \parallel 30 \text{ mH} = 7.5 \text{ mH}$   
 $L_3 + L_2 \parallel L_4 = 47 \text{ mH} + 7.5 \text{ mH} = 54.5 \text{ mH}$   
 $54.5 \text{ mH} \parallel 22 \text{ mH} = 15.67 \text{ mH}$   
 $L_T = L_1 + 15.67 \text{ mH} = 18 \text{ mH} + 15.67 \text{ mH} = \mathbf{33.67 \text{ mH}}$

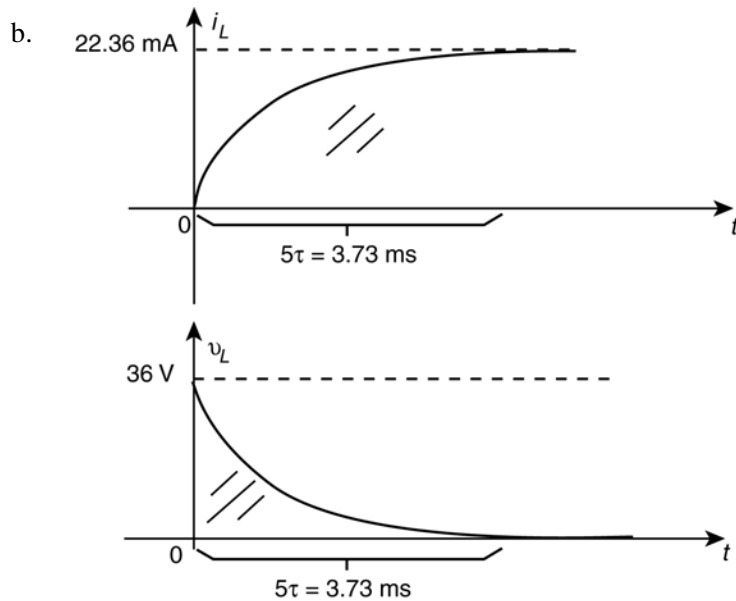
39.  $33 \text{ mH} + 1.8 \text{ mH} = 5.1 \text{ mH}$   
 $4.7 \text{ mH} \parallel 5.1 \text{ mH} = \mathbf{2.45 \text{ mH}}$



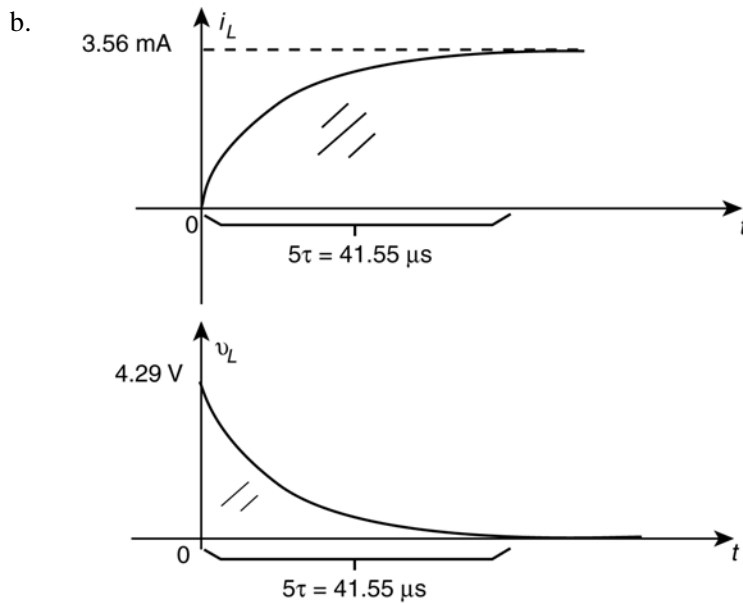
40.  $L'_T = 6.2 \text{ mH} + 12 \text{ mH} \parallel 36 \text{ mH} + 24 \text{ mH} = \mathbf{39.2 \text{ mH}}$   
 $C'_T = 9.1 \mu\text{F} + 10 \mu\text{F} \parallel 91 \mu\text{F} = 9.1 \mu\text{F} + 9.01 \mu\text{F} = 18.11 \mu\text{F}$   
 $C_T = C'_T \parallel 3.3 \mu\text{F} = 18.11 \mu\text{F} \parallel 3.3 \mu\text{F} = 2.79 \mu\text{F}$   
**39.2 mH in series with 2.79 μF**

41.  $7 \mu\text{F} \parallel 42 \mu\text{F} = 6 \mu\text{F}$   
 $12 \mu\text{F} + 6 \mu\text{F} = \mathbf{18 \mu\text{F}}$   
 $5 \text{ mH} + 20 \text{ mH} = \mathbf{25 \text{ mH}}$   
 Series combination of 2.2 kΩ resistor, 25 mH coil, 18 μF capacitor

42. a.  $R'_T = 2 \text{ k}\Omega \parallel 8.2 \text{ k}\Omega = 1.61 \text{ k}\Omega$ ,  $L'_T = 3 \text{ mH} \parallel 2 \text{ mH} = 1.2 \text{ mH}$   
 $\tau = \frac{L'_T}{R'_T} = \frac{1.2 \text{ mH}}{1.61 \text{ k}\Omega} = 745.3 \mu\text{s}$   
 $i_L = \frac{E}{R'_T}(1 - e^{-t/\tau})$   
 $= \frac{36 \text{ V}}{1.61 \text{ k}\Omega}(1 - e^{-t/745.3 \mu\text{s}}) = \mathbf{22.36 \text{ mA}(1 - e^{-t/745.3 \mu\text{s}})}$   
 $v_L = Ee^{-t/\tau} = \mathbf{36 \text{ V}e^{-t/745.3 \mu\text{s}}}$



43. a. Source conversion:  $E = 16 \text{ V}$ ,  $R_s = 2 \text{ k}\Omega$   
 $R_{Th} = 2 \text{ k}\Omega + 2 \text{ k}\Omega \parallel 8.2 \text{ k}\Omega = 2 \text{ k}\Omega + 1.61 \text{ k}\Omega = 3.61 \text{ k}\Omega$   
 $E_{Th} = \frac{8.2 \text{ k}\Omega(16 \text{ V})}{8.2 \text{ k}\Omega + 2 \text{ k}\Omega} = 12.86 \text{ V}$   
 $I_m = \frac{E_{Th}}{R_{Th}} = \frac{12.86 \text{ V}}{3.61 \text{ k}\Omega} = 3.56 \text{ mA}$ ,  $\tau = \frac{L}{R} = \frac{30 \text{ mH}}{3.61 \text{ k}\Omega} = 8.31 \mu\text{s}$   
 $i_L = 3.56 \text{ mA}(1 - e^{-t/8.31\mu\text{s}})$   
 $v_{L_1} + v_{L_2} = 12.86 \text{ V}$  initially ( $t = 0+$ )  
 $v_L = \frac{10 \text{ mH}}{10 \text{ mH} + 20 \text{ mH}}$  of total  $= \frac{1}{3}(12.86 \text{ V}) = 4.29 \text{ V}$   
 $v_L = 4.29 \text{ V}e^{-t/8.31\mu\text{s}}$



44. a.
- 
- $\leftarrow R_{Th} = 10 \text{ k}\Omega \parallel 20 \text{ k}\Omega = 6.67 \text{ k}\Omega$   
 $E_{Th} = \frac{20 \text{ k}\Omega(20 \text{ V})}{20 \text{ k}\Omega + 10 \text{ k}\Omega} = 13.33 \text{ V}$

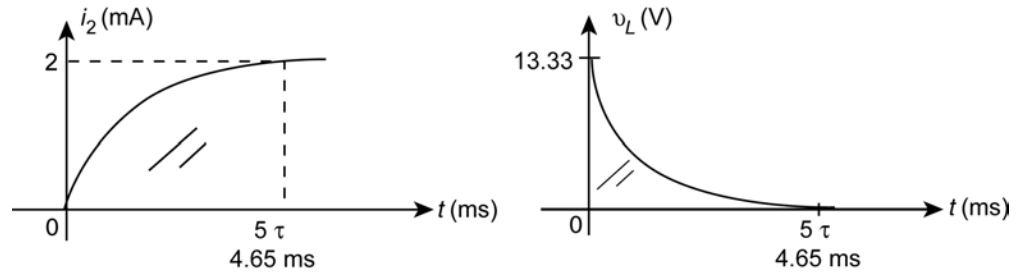
$$L_T = 3 \text{ H} + 4.7 \text{ H} \parallel 10 \text{ H} = 3 \text{ H} + 3.197 \text{ H} = \mathbf{6.197 \text{ H}}$$

$$\tau = \frac{L_T}{R} = \frac{6.197 \text{ H}}{6.67 \text{ k}\Omega} = 0.93 \text{ ms}$$

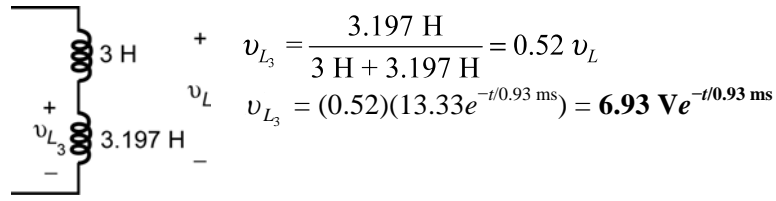
$$v_L = 13.33 \text{ V}e^{-t/0.93 \text{ ms}}$$

$$i_L = \frac{13.33 \text{ V}}{6.67 \text{ k}\Omega} (1 - e^{-t/\tau}) = \mathbf{2 \text{ mA}(1 - e^{-t/0.93 \text{ ms}})}$$

b.



c.



$$45. \quad I_{R_1} = \frac{E}{R_1} = \frac{20 \text{ V}}{4 \Omega} = 5 \text{ A}$$

$$I_2 = 0 \text{ A}$$

$$I_1 = I_{R_1} + I_2 = 5 \text{ A} + 0 \text{ A} = 5 \text{ A}$$

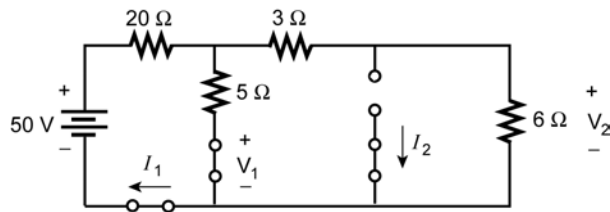
$$46. \quad I_1 = I_2 = 0 \text{ A}$$

$$V_1 = V_2 = E = 60 \text{ V}$$

$$47. \quad I_1 = \frac{12 \text{ V}}{4 \Omega} = 3 \text{ A}, \quad I_2 = 0 \text{ A}$$

$$V_1 = 12 \text{ V}, \quad V_2 = 0 \text{ V}$$

48.



$$V_2 = \frac{6 \Omega(50 \text{ V})}{6 \Omega + 20 \Omega + 3 \Omega} = 10.34 \text{ V}$$

$$V_1 = \frac{(3 \Omega + 6 \Omega)(50 \text{ V})}{29 \Omega} = 15.52 \text{ V}$$

$$I_1 = \frac{50 \text{ V}}{20 \Omega + 3 \Omega + 6 \Omega} = 1.72 \text{ A}$$

$$I_2 = 0 \text{ A}$$