

- c.  $I_1: P = V_1 I_1 = (4.8 \text{ V})(4 \text{ A}) = \mathbf{19.2 \text{ W}}$   
 $I_2: P = |(V_1 - V_2)I_2| = |(4.8 \text{ V} - 6.4 \text{ V})(2 \text{ A})| = \mathbf{3.2 \text{ W}}$

44.

- a.  $\begin{matrix} V_1 & V_2 \\ \circ & \circ \end{matrix}$

At  $V_1$ :  $\Sigma I_i = \Sigma I_o$

$$0 = 6 \text{ A} + \frac{V_1}{5 \Omega} + \frac{V_1 - V_2}{3 \Omega} + \frac{V_1 - V_2}{2 \Omega}$$

At  $V_2$ :  $\Sigma I_i = \Sigma I_o$

$$7 \text{ A} + \frac{V_1 - V_2}{3 \Omega} + \frac{V_1 - V_2}{2 \Omega} = \frac{V_2}{4 \Omega} + \frac{V_2}{8 \Omega}$$

so that  $V_1 \left[ \frac{1}{5 \Omega} + \frac{1}{3 \Omega} + \frac{1}{2 \Omega} \right] - V_2 \left[ \frac{1}{3 \Omega} + \frac{1}{2 \Omega} \right] = -6 \text{ A}$

$$V_2 \left[ \frac{1}{4 \Omega} + \frac{1}{8 \Omega} + \frac{1}{3 \Omega} + \frac{1}{2 \Omega} \right] - V_1 \left[ \frac{1}{3 \Omega} + \frac{1}{2 \Omega} \right] = 7 \text{ A}$$

---

or  $1.03V_1 - 0.833V_2 = -6$   
 $-0.833V_1 + 1.21V_2 = 7$

---

- b.  $V_1 = \mathbf{-2.59 \text{ V}}$ ,  $V_2 = \mathbf{4 \text{ V}}$
- c.  $V_{2\Omega} = V_{3\Omega} = V_2 - V_1 = 4 \text{ V} - (-2.59 \text{ V}) = \mathbf{6.59 \text{ V}}$   
 $V_{5\Omega} = V_1 = \mathbf{-2.59 \text{ V}}$   
 $V_{4\Omega} = V_{8\Omega} = V_2 = \mathbf{4 \text{ V}}$

45.

- a.  $\begin{matrix} V_1 & V_2 \\ \circ & \circ \end{matrix}$

Source conversion:  $I_3 = \frac{12 \text{ V}}{4 \Omega} = 3 \text{ A}$ ,  $R_p = R_3 = 4 \Omega$

At  $V_1$ :  $\Sigma I_i = \Sigma I_o$

$$0 = \frac{V_1}{3 \Omega} + \frac{V_1}{6 \Omega} + 5 \text{ A} + \frac{V_1 - V_2}{4 \Omega} + 3 \text{ A}$$

At  $V_2$ :  $\Sigma I_i = \Sigma I_o$

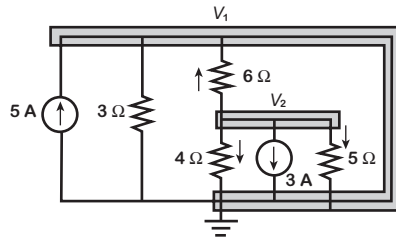
$$3 \text{ A} + \frac{V_1 - V_2}{4 \Omega} = \frac{V_2}{8 \Omega} + 4 \text{ A}$$

Rewritten:  $V_1 \left[ \frac{1}{3 \Omega} + \frac{1}{6 \Omega} + \frac{1}{4 \Omega} \right] - \frac{V_2}{4 \Omega} = -5 \text{ A} - 3 \text{ A}$

$$-V_1 \left[ \frac{1}{4 \Omega} \right] + V_2 \left[ \frac{1}{4 \Omega} + \frac{1}{8 \Omega} \right] = -4 \text{ A} + 3 \text{ A}$$

- b.  $V_1 = \mathbf{-14.86 \text{ V}}$ ,  $V_2 = \mathbf{-12.57 \text{ V}}$
- c.  $I_{6\Omega} \uparrow = \frac{14.86 \text{ V}}{6 \Omega} = \mathbf{2.48 \text{ A}}$

46. a. Source conversion:  $I_s = \frac{15 \text{ V}}{3 \Omega} = 5 \text{ A}$ ,  $R_p = 3 \Omega$



- b.  $V_1 = 0 \text{ V}$  (tied to ground)

$$\sum I_i = \sum I_o$$

$$0 = \frac{V_2}{6 \Omega} + \frac{V_2}{4 \Omega} + \frac{V_2}{5 \Omega} + 3 \text{ A}$$

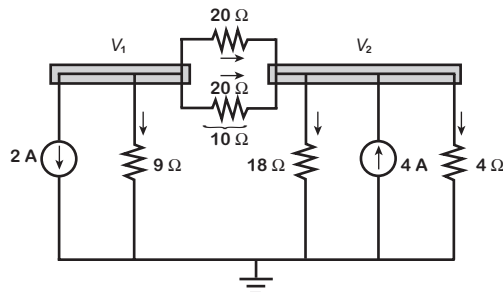
$$\text{and } V_2 \left[ \frac{1}{6 \Omega} + \frac{1}{4 \Omega} + \frac{1}{5 \Omega} \right] = -3 \text{ A}$$

$$V_2 [616.67 \text{ mS}] = -3 \text{ A}$$

$$V_2 = -\frac{3 \text{ A}}{616.67 \text{ mS}} = \mathbf{4.86 \text{ V}}$$

- c.  $V_{2-}^+ = \mathbf{-4.86 \text{ V}}$

47. a.



$$V_1: \sum I_i = \sum I_o$$

$$0 = 2 \text{ A} + \frac{V_1}{9 \Omega} + \frac{V_1 - V_2}{10 \Omega}$$

$$V_2: \sum I_i = \sum I_o$$

$$\frac{V_1 - V_2}{10 \Omega} + 4 \text{ A} = \frac{V_2}{18 \Omega} + \frac{V_2}{4 \Omega}$$

---


$$0.211 V_1 - 0.1 V_2 = -2$$

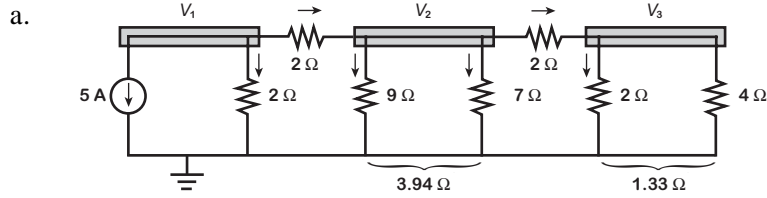
$$-0.1 V_1 + 0.405 V_2 = 4$$


---

- b.  $V_1 = \mathbf{-5.43 \text{ V}}$ ,  $V_2 = \mathbf{8.53 \text{ V}}$

$$\begin{aligned}
 c. \quad V_{R_4} &= V_1 - V_2 \\
 &= (-5.43 \text{ V}) - (8.53 \text{ V}) \\
 &= \mathbf{-13.96 \text{ V}}
 \end{aligned}$$

48.



$$V_1: \Sigma I_i = \Sigma I_o$$

$$0 = 5 \text{ A} + \frac{V_1}{2 \Omega} + \frac{V_1 - V_2}{2 \Omega}$$

$$V_2: \Sigma I_i = \Sigma I_o$$

$$\frac{V_1 - V_2}{2 \Omega} = \frac{V_2}{3.94 \Omega} + \frac{V_2 - V_3}{2 \Omega}$$

$$V_3: \Sigma I_i = \Sigma I_o$$

$$\frac{V_2 - V_3}{2 \Omega} = \frac{V_3}{1.33 \Omega}$$

b.  $V_1 = \mathbf{-6.556 \text{ V}}$ ,  $V_2 = \mathbf{-3.113 \text{ V}}$   
 $V_3 = \mathbf{-1.245 \text{ V}}$

c.  $I_{9\Omega} = \frac{V_2}{9 \Omega} = \frac{3.113 \text{ V}}{9 \Omega} = \mathbf{0.346 \text{ A} \uparrow}$

49.

a.  $\circ V_1$     $\circ V_2$

$\circ V_3$

$$\text{At } V_1: \Sigma I_i = \Sigma I_o$$

$$0 = 5 \text{ A} + \frac{V_1}{2 \Omega} + \frac{V_1 - V_3}{6 \Omega}$$

$$\text{At } V_2: \Sigma I_i = \Sigma I_o$$

$$5 \text{ A} = 2 \text{ A} + \frac{V_2}{4 \Omega}$$

$$\text{At } V_3: \Sigma I_i = \Sigma I_o$$

$$\frac{V_1 - V_3}{6 \Omega} + 2 \text{ A} + \frac{V_3}{5 \Omega}$$

Rewritten:

$$V_1 \left[ \frac{1}{2 \Omega} + \frac{1}{6 \Omega} \right] - \frac{1}{6 \Omega} V_3 = -5 \text{ A}$$

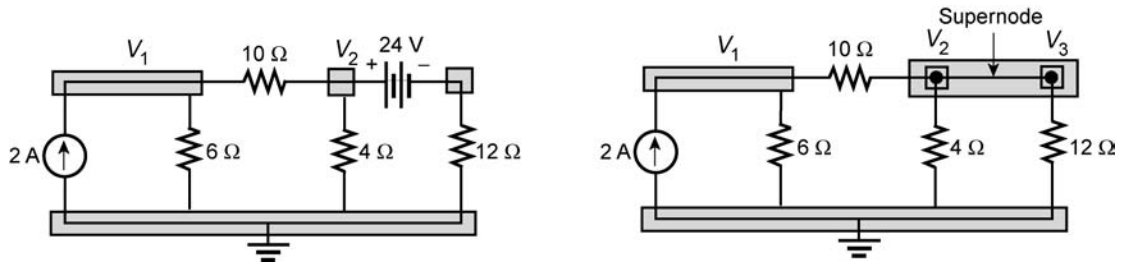
$$V_2 \left[ \frac{1}{4 \Omega} \right] = 5 \text{ A} - 2 \text{ A}$$

$$V_3 \left[ \frac{1}{6 \Omega} + \frac{1}{5 \Omega} \right] - \frac{1}{6 \Omega} V_1 = 2 \text{ A}$$

b.  $V_1 = -6.92 \text{ V}$ ,  $V_2 = 12 \text{ V}$ ,  $V_3 = 2.3 \text{ V}$

c.  $I_{4\Omega} = \frac{V_1}{4 \Omega} = \frac{12 \text{ V}}{4 \Omega} = 3 \text{ A}$

50. a.



$$\Sigma I_i = \Sigma I_o$$

Node  $V_1$ :

$$2 \text{ A} = \frac{V_1}{6 \Omega} + \frac{V_1 - V_2}{10 \Omega}$$

Supernode  $V_2, V_3$ :

$$0 = \frac{V_2 - V_1}{10 \Omega} + \frac{V_2}{4 \Omega} + \frac{V_3}{12 \Omega}$$

Independent source:

$$V_2 - V_3 = 24 \text{ V} \text{ or } V_3 = V_2 - 24 \text{ V}$$

2 eq. 2 unknowns:

$$\frac{V_1}{6 \Omega} + \frac{V_1 - V_2}{10 \Omega} = 2 \text{ A}$$

$$\frac{V_2 - V_1}{10 \Omega} + \frac{V_2}{4 \Omega} + \frac{V_2 - 24 \text{ V}}{12 \Omega} = 0$$

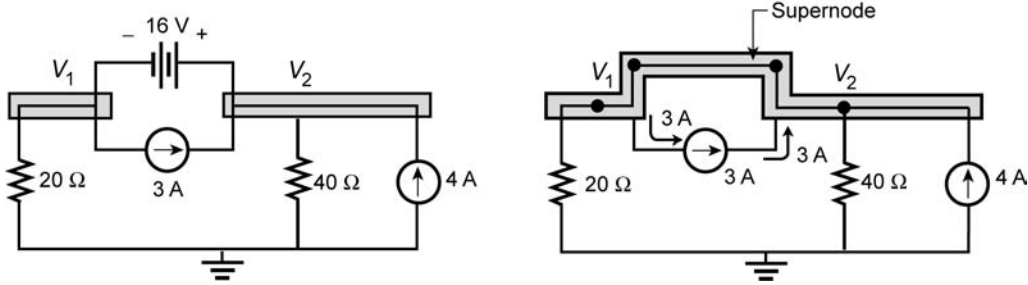
$$0.267V_1 - 0.1V_2 = 2$$

$$+0.1V_1 - 0.433V_2 = -2$$

$$V_1 = 10.08 \text{ V}, V_2 = 6.94 \text{ V}$$

$$V_3 = V_2 - 24 \text{ V} = -17.06 \text{ V}$$

51.



$$\Sigma I_i = \Sigma I_o$$

Supernode:

$$3 \text{ A} + 4 \text{ A} = 3 \text{ A} + \frac{V_1}{20 \Omega} + \frac{V_2}{40 \Omega}$$

$$2 \text{ eq. } 2 \text{ unk. } \begin{cases} 4 \text{ A} = \frac{V_1}{20 \Omega} + \frac{V_2}{40 \Omega} \\ V_2 - V_1 = 16 \text{ V} \end{cases}$$

$$\text{Subst. } V_2 = 16 \text{ V} + V_1$$

$$4 \text{ A} = \frac{V_1}{20 \Omega} + \frac{(16 \text{ V} + V_1)}{40 \Omega}$$

$$\text{and } V_1 = \mathbf{48 \text{ V}}$$

$$V_2 = 16 \text{ V} + V_1 = \mathbf{64 \text{ V}}$$

52.

$$\begin{array}{l} \text{a.} \\ \begin{array}{c} V_1 \\ \circ \\ V_2 \\ \circ \end{array} \\ V_1 \left[ \frac{1}{2} + \frac{1}{8} \right] - V_2 \left[ \frac{1}{8} \right] = -5 \\ -V_1 \left[ \frac{1}{8} \right] + V_2 \left[ \frac{1}{8} + \frac{1}{4} \right] = -3 \end{array}$$

$$V_1 = \mathbf{-10.27 \text{ V}}, V_2 = \mathbf{-11.36 \text{ V}}$$

$$\text{b. } V_{I_1} = V_1 = \mathbf{-10.27 \text{ V}}, V_{I_2} = V_2 = \mathbf{-11.36 \text{ V}}$$

53.

$$\begin{array}{l} \text{a.} \\ \begin{array}{c} V_1 \\ \circ \\ V_2 \\ \circ \end{array} \\ V_1 \left[ \frac{1}{8} + \frac{1}{6} \right] - V_2 \left[ \frac{1}{6} \right] = -12 \text{ A} + 9 \text{ A} = -3 \text{ A} \\ V_2 \left[ \frac{1}{20} + \frac{1}{5} + \frac{1}{6} \right] - V_1 \left[ \frac{1}{6} \right] = -9 \text{ A} \end{array}$$

$$V_1 = \mathbf{-29.29 \text{ V}}, V_2 = \mathbf{-33.34 \text{ V}}$$

$$\begin{aligned} \text{b. } V_1 - V_{6\Omega} - 54 \text{ V} - V_2 &= 0 \\ V_{6\Omega} &= V_1 - V_2 - 54 \text{ V} = -29.29 \text{ V} - (-33.34 \text{ V}) - 54 \text{ V} = \mathbf{-49.95 \text{ V}} \\ &\quad \begin{matrix} + & - \end{matrix} \end{aligned}$$

$$\begin{aligned} 54. \quad \text{a. } V_1 \left[ \frac{1}{9 \Omega} + \frac{1}{10 \Omega} \right] - V_2 \left[ \frac{1}{10 \Omega} \right] &= -2 \text{ A} \\ V_2 \left[ \frac{1}{10 \Omega} + \frac{1}{18 \Omega} + \frac{1}{4 \Omega} \right] - V_1 \left[ \frac{1}{10 \Omega} \right] &= 4 \text{ A} \end{aligned}$$

$$\begin{aligned} \text{b. } V_1 \left[ \frac{1}{9 \Omega} + \frac{1}{10 \Omega} \right] - V_2 \left[ \frac{1}{10 \Omega} \right] &= -2 \text{ A} \\ -V_1 \left[ \frac{1}{10 \Omega} \right] + V_2 \left[ \frac{1}{10 \Omega} + \frac{1}{18 \Omega} + \frac{1}{4 \Omega} \right] &= 4 \text{ A} \end{aligned}$$

---


$$\begin{aligned} 0.211 V_1 - 0.1 V_2 &= -2 \\ -0.1 V_1 + .405 V_2 &= 4 \end{aligned}$$


---

$$\text{c. } V_1 = \mathbf{-5.43 \text{ V}}, V_2 = \mathbf{8.53 \text{ V}}$$

$$\text{d. } I_{4\Omega} = \frac{V_2}{4 \Omega} = \frac{8.53 \text{ V}}{4 \Omega} = \mathbf{2.13 \text{ A} \downarrow}$$

$$\begin{aligned} 55. \quad \text{a. } V_1 \left[ \frac{1}{2 \Omega} + \frac{1}{2 \Omega} \right] - V_2 \left[ \frac{1}{2 \Omega} \right] &= -5 \text{ A} \\ V_2 \left[ \frac{1}{2 \Omega} + \frac{1}{9 \Omega} + \frac{1}{7 \Omega} + \frac{1}{2 \Omega} \right] - V_1 \left[ \frac{1}{2 \Omega} \right] - V_3 \left[ \frac{1}{2 \Omega} \right] &= 0 \\ V_3 \left[ \frac{1}{2 \Omega} + \frac{1}{2 \Omega} + \frac{1}{4 \Omega} \right] - V_2 \left[ \frac{1}{2 \Omega} \right] &= 0 \end{aligned}$$

---


$$\begin{aligned} V_1 &= \mathbf{-6.556 \text{ V}}, V_2 = \mathbf{-3.113 \text{ V}} \\ V_3 &= \mathbf{-1.245 \text{ V}} \end{aligned}$$

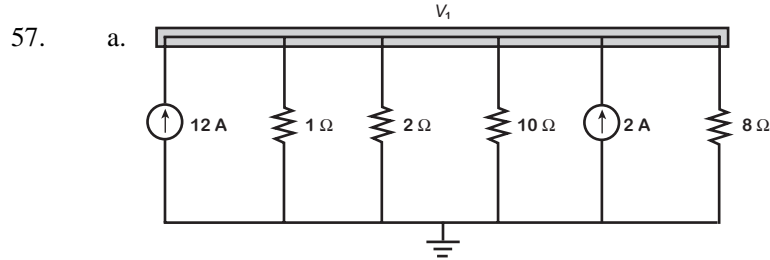
$$\text{b. } I_{9\Omega} = \frac{V_2}{9 \Omega} = \frac{-3.113 \text{ V}}{9 \Omega} = \mathbf{0.346 \text{ A} \uparrow}$$

$$\begin{aligned} 56. \quad \text{a. } V_1 \left[ \frac{1}{2 \Omega} + \frac{1}{6 \Omega} \right] - \frac{1}{6 \Omega} V_3 &= -5 \text{ A} \\ V_2 \left[ \frac{1}{4 \Omega} \right] &= 5 \text{ A} - 2 \text{ A} \\ V_3 \left[ \frac{1}{6 \Omega} + \frac{1}{5 \Omega} \right] - \frac{1}{6 \Omega} V_1 &= 2 \text{ A} \end{aligned}$$


---

b.  $V_1 = -6.92 \text{ V}$ ,  $V_2 = 12 \text{ V}$ ,  $V_3 = 2.3 \text{ V}$

c.  $I_{2\Omega} = \frac{V_2}{2 \Omega} = \frac{6.92 \text{ V}}{2 \Omega} = 3.46 \text{ A}$



$$V_1 \left[ \frac{1}{1 \Omega} + \frac{1}{2 \Omega} + \frac{1}{10 \Omega} + \frac{1}{8 \Omega} \right] = 14 \text{ A}$$

$$V_1 [1.725 \text{ S}] = 14 \text{ A}$$

$$V_1 = \frac{14}{1.725} \text{ V}$$

$$= 8.1 \text{ V}$$

b.  $V_a = 0 \text{ V}$ ,  $V_b = 8.12 \text{ V}$   
 $V_{ab} = V_a - V_b = 0 \text{ V} - 8.12 \text{ V} = -8.12 \text{ V}$

58. a. Same figure used for problem 46.

$$V_1 = 0 \text{ V}$$

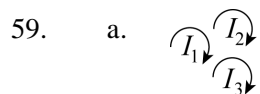
$$V_2 \left[ \frac{1}{6 \Omega} + \frac{1}{4 \Omega} + \frac{1}{5 \Omega} \right] - \frac{1}{6 \Omega} V_1 = -3 \text{ A}$$

b.  $V_1 = 0 \text{ V}$   
 $\therefore V_2 [0.617 \text{ S}] = -3 \text{ A}$

$$V_2 = \frac{-3}{0.617} \text{ V}$$

$$= -4.86 \text{ V}$$

c.  $I_{5\Omega} = \frac{V_2}{5 \Omega} = \frac{4.86 \text{ V}}{5 \Omega} = .972 \text{ A}$



$$I_1(6 \Omega + 2 \Omega + 10 \Omega) - 2 \Omega I_2 - 10 \Omega I_3 = 12 \text{ V}$$

$$I_2(2 \Omega + 2 \Omega + 5 \Omega) - 5 \Omega I_3 - 2 \Omega I_1 = 0$$

$$I_3(5 \Omega + 20 \Omega + 10 \Omega) - 5 \Omega I_2 - 10 \Omega I_1 = 0$$

$$18I_1 - 2I_2 - 10I_3 = 12$$

$$-2I_1 + 9I_2 - 5I_3 = 0$$

$$-10I_1 - 5I_2 + 35I_3 = 0$$

---

b.  $I_{5\Omega} = I_2 - I_3 = 0.362 \text{ A} - 0.302 \text{ A} = \mathbf{60 \text{ mA}}$

c. **no**

d. **no**

60. a.  $\circ V_1$

$\circ V_2$        $\circ V_3$

$$V_1 \left[ \frac{1}{6 \Omega} + \frac{1}{2 \Omega} + \frac{1}{5 \Omega} \right] - \frac{1}{2 \Omega} V_2 - \frac{1}{5 \Omega} V_3 = 2 \text{ A}$$

$$V_2 \left[ \frac{1}{2 \Omega} + \frac{1}{5 \Omega} + \frac{1}{10 \Omega} \right] - \frac{1}{2 \Omega} V_1 - \frac{1}{5 \Omega} V_3 = 0$$

$$V_3 \left[ \frac{1}{5 \Omega} + \frac{1}{5 \Omega} + \frac{1}{20 \Omega} \right] - \frac{1}{5 \Omega} V_2 - \frac{1}{5 \Omega} V_1 = 0$$


---

or  $0.867V_1 - 0.5V_2 - 0.2V_3 = 12$

$-0.5V_1 + 0.8V_2 - 0.2V_3 = 0$

$-0.2V_1 - 0.2V_2 + 0.45V_3 = 0$

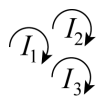
---

$V_2 = \mathbf{5.7 \text{ V}}, V_3 = \mathbf{5.6 \text{ V}}$

b.  $V_{5\Omega} = V_2 - V_3 = 5.7 \text{ V} - 5.6 \text{ V} = \mathbf{0.1 \text{ V}}$

c. **no**

d. **no**  $2 \Omega / 10 \Omega = \frac{1}{5} \neq 5 \Omega / 20 \Omega = \frac{1}{4}$

61. a. 

Source conversion:  $E = IR = (12 \text{ m})(2 \text{ k}\Omega) = 24 \text{ V}$

$R_s = 2 \text{ k}\Omega$

$I_1(2 \text{ k}\Omega + 33 \text{ k}\Omega + 3.3 \text{ k}\Omega) - 33 \text{ k}\Omega I_2 - 3.3 \text{ k}\Omega I_3 = 24 \text{ V}$

$I_2(33 \text{ k}\Omega + 56 \text{ k}\Omega + 36 \text{ k}\Omega) - 33 \text{ k}\Omega I_1 - 36 \text{ k}\Omega I_3 = 0$

$I_3(36 \text{ k}\Omega + 3.3 \text{ k}\Omega + 5.6 \text{ k}\Omega) - 3.3 \text{ k}\Omega I_1 - 36 \text{ k}\Omega I_2 = 0$

---

$I_1 = \mathbf{0.97 \text{ mA}}, I_2 = I_3 = \mathbf{0.36 \text{ mA}}$

b.  $I_5 = I_2 - I_3 = 0.36 \text{ mA} - 0.36 \text{ mA} = \mathbf{0 \text{ mA}}$

c, d. **yes**



62. a.  $\begin{matrix} \circ V_1 \\ \circ V_2 \quad \circ V_3 \end{matrix}$

$$V_1 \left[ \frac{1}{2 \text{ k}\Omega} + \frac{1}{33 \text{ k}\Omega} + \frac{1}{56 \text{ k}\Omega} \right] - \frac{1}{33 \text{ k}\Omega} V_2 - \frac{1}{56 \text{ k}\Omega} V_3 = 12 \text{ mA}$$

$$V_2 \left[ \frac{1}{33 \text{ k}\Omega} + \frac{1}{3.3 \text{ k}\Omega} + \frac{1}{36 \text{ k}\Omega} \right] - \frac{1}{33 \text{ k}\Omega} V_1 - \frac{1}{36 \text{ k}\Omega} V_3 = 0$$

$$V_3 \left[ \frac{1}{56 \text{ k}\Omega} + \frac{1}{36 \text{ k}\Omega} + \frac{1}{5.6 \text{ k}\Omega} \right] - \frac{1}{36 \text{ k}\Omega} V_2 - \frac{1}{56 \text{ k}\Omega} V_1 = 0$$


---

Rewritten:  $548.16V_1 - 30.3V_2 - 17.86V_3 = 12 \times 10^3$   
 $-30.3V_1 + 361.11V_2 - 27.78V_3 = 0$   
 $-17.86V_1 - 27.78V_2 + 224.21V_3 = 0$

---

$$V_2 = \mathbf{2.01 \text{ V}}, V_3 = \mathbf{2.01 \text{ V}}$$

b.  $V_{R_5} = V_2 - V_3 = 2.01 \text{ V} - 2.01 \text{ V} = \mathbf{0 \text{ V}}$

c, d. **yes**

63. Mesh Analysis

$$\begin{matrix} I_2 \downarrow \\ I_1 \downarrow \\ I_3 \downarrow \end{matrix} \quad \begin{aligned} (1 \text{ k}\Omega + 2 \text{ k}\Omega + 2 \text{ k}\Omega)I_1 - 2 \text{ k}\Omega I_2 - 2 \text{ k}\Omega I_3 &= 10 \\ (2 \text{ k}\Omega + 2 \text{ k}\Omega + 2 \text{ k}\Omega)I_2 - 2 \text{ k}\Omega I_1 - 2 \text{ k}\Omega I_3 &= 0 \\ (2 \text{ k}\Omega + 2 \text{ k}\Omega + 2 \text{ k}\Omega)I_3 - 2 \text{ k}\Omega I_1 - 2 \text{ k}\Omega I_2 &= 0 \end{aligned}$$


---

$$I_1 = I_{10\text{V}} = \mathbf{3.33 \text{ mA}}$$

Nodal Analysis:

Source conversion:  $I = 10 \text{ V}/1 \text{ k}\Omega = 10 \text{ mA}$ ,  $R = 1 \text{ k}\Omega$

$$\begin{matrix} \circ V_1 \\ \circ V_3 \quad \circ V_2 \end{matrix} \quad V_1 \left[ \frac{1}{1 \text{ k}\Omega} + \frac{1}{2 \text{ k}\Omega} + \frac{1}{2 \text{ k}\Omega} \right] - \frac{1}{2 \text{ k}\Omega} V_2 - \frac{1}{2 \text{ k}\Omega} V_3 = 10 \text{ mA}$$

$$\begin{matrix} \oplus \\ \ominus \end{matrix} \quad V_2 \left[ \frac{1}{2 \text{ k}\Omega} + \frac{1}{2 \text{ k}\Omega} + \frac{1}{2 \text{ k}\Omega} \right] - \frac{1}{2 \text{ k}\Omega} V_1 - \frac{1}{2 \text{ k}\Omega} V_3 = 0$$

$$V_3 \left[ \frac{1}{2 \text{ k}\Omega} + \frac{1}{2 \text{ k}\Omega} + \frac{1}{2 \text{ k}\Omega} \right] - \frac{1}{2 \text{ k}\Omega} V_2 - \frac{1}{2 \text{ k}\Omega} V_1 = 0$$

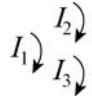

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$$V_1 = 6.67 \text{ V} = E - IR_s = 10 \text{ V} - I(1 \text{ k}\Omega)$$

$$I = \frac{10 - 6.67 \text{ V}}{1 \text{ k}\Omega} = \mathbf{3.33 \text{ mA}}$$

64.

Mesh Analysis



Source conversion:  $E = 20 \text{ V}$ ,  $R = 10 \Omega$

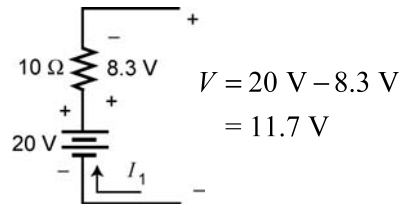
$$(10 + 10 + 20)I_1 - 10I_2 - 20I_3 = 20$$

$$(10 + 20 + 20)I_2 - 10I_1 - 20I_3 = 0$$

$$(20 + 20 + 10)I_3 - 20I_1 - 20I_2 = 0$$

---


$$I_1 = I_{20\text{V}} = 0.83 \text{ A}$$



$$I_s = \frac{V}{R_s} = \frac{11.70 \text{ V}}{10 \Omega} = \mathbf{1.17 \text{ A}}$$

Nodal Analysis:

$$\begin{matrix} \circ V_1 \\ \circ V_3 & \circ V_2 \\ \text{---} \end{matrix} \quad V_1 \left[ \frac{1}{10} + \frac{1}{10} + \frac{1}{20} \right] - \left[ \frac{1}{20} \right] V_2 - \left[ \frac{1}{10} \right] V_3 = 2$$

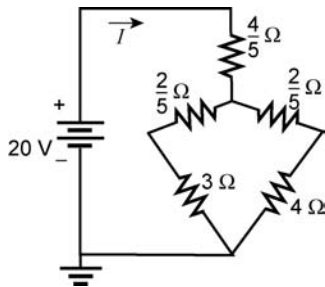
$$V_2 \left[ \frac{1}{20} + \frac{1}{20} + \frac{1}{10} \right] - \left[ \frac{1}{20} \right] V_1 - \left[ \frac{1}{20} \right] V_3 = 0$$

$$V_3 \left[ \frac{1}{10} + \frac{1}{20} + \frac{1}{20} \right] - \left[ \frac{1}{10} \right] V_1 - \left[ \frac{1}{20} \right] V_2 = 0$$

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$$I_{R_s} = \frac{V_1}{R_s} = \mathbf{1.17 \text{ A}}$$

65.

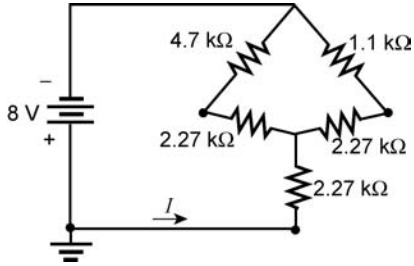


$$I = \frac{20 \text{ V}}{\frac{4}{5} \Omega + \left[ \frac{2}{5} \Omega + 3 \Omega \right] \parallel \left[ \frac{2}{5} \Omega + 4 \Omega \right]}$$

$$= \frac{20 \text{ V}}{\frac{4}{5} \Omega + (3.14 \Omega) \parallel (4.4 \Omega)}$$

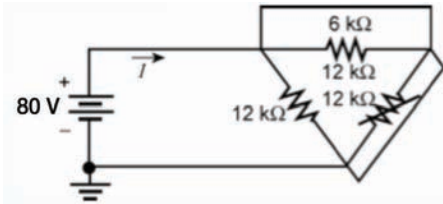
$$= \mathbf{7.36 \text{ A}}$$

66.



$$\begin{aligned}
 R_T &= 2.27 \text{ k}\Omega + [4.7 \text{ k}\Omega + 2.27 \text{ k}\Omega] \parallel [1.1 \text{ k}\Omega + 2.27 \text{ k}\Omega] \\
 &= 2.27 \text{ k}\Omega + [6.97 \text{ k}\Omega] \parallel [3.37 \text{ k}\Omega] \\
 &= 2.27 \text{ k}\Omega + 2.27 \text{ k}\Omega \\
 &= 4.54 \text{ k}\Omega \\
 I &= \frac{8 \text{ V}}{4.54 \text{ k}\Omega} = \mathbf{1.76 \text{ mA}}
 \end{aligned}$$

67.



(Y-Δ conversion)

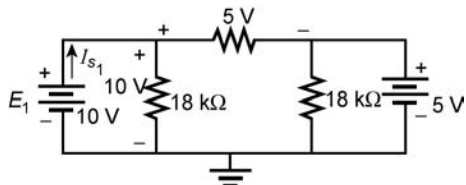
$$\begin{aligned}
 I &= \frac{80 \text{ V}}{12 \text{ k}\Omega \parallel 12 \text{ k}\Omega \parallel 6 \text{ k}\Omega} = \frac{80 \text{ V}}{3 \text{ k}\Omega} \\
 &= \mathbf{26.67 \text{ mA}}
 \end{aligned}$$

68.

$$\begin{aligned}
 \text{a. } I &= \frac{42 \text{ V}}{(18 \Omega \parallel 18 \Omega) \parallel [(18 \Omega \parallel 18 \Omega) + (18 \Omega \parallel 18 \Omega)]} = \frac{42 \text{ V}}{9 \Omega \parallel [9 \Omega + 9 \Omega]} \\
 &= \mathbf{7 \text{ A}} \text{ (Y-}\Delta \text{ conversion)}
 \end{aligned}$$

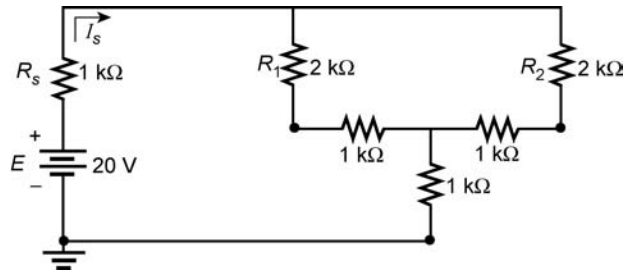
b. Δ - Y conversion

69.



$$I_{s_1} = \frac{10 \text{ V}}{18 \text{ k}\Omega} + \frac{5 \text{ V}}{18 \text{ k}\Omega} = \frac{15 \text{ V}}{18 \text{ k}\Omega} = \mathbf{0.83 \text{ mA}}$$

70. a.



b.

$$R' = R_1 + 1 \text{ k}\Omega = 3 \text{ k}\Omega$$

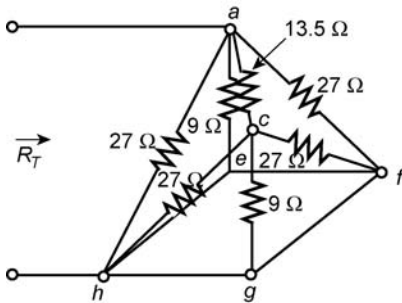
$$R'' = R_2 + 1 \text{ k}\Omega = 3 \text{ k}\Omega$$

$$R'_T = \frac{3 \text{ k}\Omega}{2} = 1.5 \text{ k}\Omega$$

$$R_T = 1 \text{ k}\Omega + 1.5 \text{ k}\Omega + 1 \text{ k}\Omega = 3.5 \text{ k}\Omega$$

$$I_s = \frac{E}{R_T} = \frac{20 \text{ V}}{3.5 \text{ k}\Omega} = \mathbf{5.71 \text{ mA}}$$

71. Using two  $\Delta - Y$  conversions:



$$c - g: 27 \Omega \parallel 9 \Omega \parallel 27 \Omega = 5.4 \Omega$$

$$a - h: 27 \Omega \parallel 9 \Omega \parallel 27 \Omega = 5.4 \Omega$$

$$R_T = 5.4 \Omega \parallel (13.5 \Omega + 5.4 \Omega)$$

$$= 5.4 \Omega \parallel 18.9 \Omega$$

$$= \mathbf{4.2 \Omega}$$